Algebraic Data Types Lab 3

1 Introduction: how do we define new types?

In Haskell we can define new data types. For example, we can define our own type that models various mobile devices we use:

Observația 1.1. • The data keyword is used to create a new type;

- Before = we have the name of the newly created type: MobileDevice;
- After = we have the definition of *value constructors*, which start with a capital letter and are separated by the symbol |: Smartphone, Laptop and Tablet.

Exercitial 1.2. Load into ghci a file containing the definition of the MobileDevice type. What are the types for Smartphone, Laptop and Tablet?

The type Bool, which is already defined in Haskell, looks like this: data Bool = False | True

If you try to evaluate in ghci directly the value True notice that ghci displays the value True:

cmd > True True

However, for a value of type MobileDevice we do not have the same behavior:

```
cmd > Laptop
<interactive>:11:1: error:
• No instance for (Show MobileDevice) arising from a use of 'print'
• In a stmt of an interactive GHCi command: print it
```

We get this error because ghci does not associate a string representation of the Laptop value. To solve this problem, one solution is to add deriving (Show) to the type definition like this:

Regarding the phrase deriving (Show), we only need to know for now that it allows constructing string representations for values of this type. We will discuss this construction at length in the next course. After reloading the definition, in ghci we get the expected behavior:

cmd > Laptop Laptop

For now we've defined a new data type that has only three possible values: Smartphone, Laptop, and Tablet. We generally want to be able to construct types that have multiple values. For example, we can have tablets of different sizes. To achieve this, we can add new *fields* to the value constructors:

Notice that for the Tablet constructor we added a field of type Int. This will allow us to construct more values of type MobileDevice:

```
cmd> :t (Tablet 12)
(Tablet 12) :: MobileDevice
cmd> :t (Tablet 15)
(Tablet 15) :: MobileDevice
```

For a constructor we can add multiple fields. For example, we can extend the above definition to also attach the brand of the tablets:

Exercițiul 1.3. Create a data type Colors that contains some colors. Next, change the MobileDevice type so that you can attach colors for each device.

As expected, we can also define functions on top of the new data types. When we want to write a function over a datatype of our own creation, we will use *pattern matching* over the type's values. We will explain this with an example: suppose we want to write a function that will return for each device a description. Considering the first definition for MobileDevice, the function will be implemented like this:

```
description :: MobileDevice -> String
description Laptop = "Acesta este un laptop de culoare roz."
description Tablet = "Aceasta este o tableta mov."
description Smartphone = "Acesta este un telefon mobil."
```

Notice that the function is defined for each individual constructor. Thus, when description is executed, the function definition corresponding to the given argument is searched for. If the argument is Smartphone, then the last line is the appropriate one.

Exercițiul 1.4. Using the Colors data type, write a function that displays the color of each device.

2 Binary trees. Binary search trees.

Exercitial 2.1. Define a data type for binary trees where nodes contain integers.

```
date Arb = Leaf | Node Integer Arb Arb deriving (Show, Eq)
```

Exercițiul 2.2. Write a recursive function minBST :: Arb -> Integer that returns the minimum element in a binary tree to search.

The function may be partial, in the sense that it is not defined for empty tree.

Hint: The minimum element is the leftmost element.

Exercițiul 2.3. Write a recursive function maxBST :: Arb -> Integer that returns the maximum element in a binary tree to search.

The function may be partial, in the sense that it is not defined for empty tree.

Hint: the maximum element is the rightmost element.

Exercitial 2.4. Write a function that checks whether a binary tree is a tree search binary.

```
isBST :: Arb -> Bool
isBST Leaf = True
...
```

Hint: for every subtree T of the given tree at input, the function tests that the root node of T is:

(A) greater than all elements in its left subtree T and

(B) less than all elements in the right subtree of T.

Assuming that the subtrees of T are already known to be binary search trees, test (A) can be implemented simply using maxBST, and test (B) using minBST.

Exercițiul 2.5. Write a function that searches for an integer value in a tree search binary.

search :: Arb -> Integer -> Bool

Exercițiul 2.6. Write a function that inserts an integer value into a binary search tree.

insert :: Arb -> Integer -> Arb

Exercitian 2.7. Write a function that deletes (an instance of) the largest element.

removeMax :: Arb -> Arb

Exercitial 2.8. Write a function that deletes (an instance of) a value of type integer in a binary search tree. You will likely use maxBST and removeMax as helper functions.

remove :: Arb -> Integer -> Arb

Exercițiul 2.9. Write functions that compute pre-order, in-order traversal and post-order of the trees.

preOrder :: Arb -> [Integer] inOrder :: Arb -> [Integer] postOrder :: Arb -> [Integer]